






Engineering single-atom angular momentum eigenstates in an optical tweezerPhilipp Lunt ^{1,*}, Paul Hill ¹, Johannes Reiter ¹, Philipp M. Preiss ^{2,3}, Maciej Gafka ¹ and Selim Jochim¹¹*Physikalisches Institut, Universität Heidelberg, Im Neuenheimer Feld 226, 69120 Heidelberg, Germany*²*Max Planck Institute of Quantum Optics, Hans-Kopfermann-Straße 1, 85748 Garching, Germany*³*Munich Center for Quantum Science and Technology, Schellingstraße 4, 80799 München, Germany*

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We engineer angular momentum eigenstates of a single atom by using an all-optical approach based on the interference of Laguerre-Gaussian beams. We confirm the imprint of angular momentum by measuring the two-dimensional density distribution and by performing Ramsey spectroscopy in a slightly anisotropic trap, which additionally reveals the sense of rotation. This article provides the experimental details on the quantum state control of angular momentum eigenstates reported in P. Lunt *et al.*, *Phys. Rev. Lett.* **133**, 253401 (2024).

DOI: [10.1103/PhysRevA.110.063315](https://doi.org/10.1103/PhysRevA.110.063315)**I. INTRODUCTION**

Quantum state engineering at the level of individual constituents forms a cornerstone of modern quantum technologies, ranging from quantum metrology [1,2] to quantum simulation [3] and computation [4]. It has enabled breakthroughs in cooling the motional degree of freedom of nanoparticles [5], ions [6], neutral atoms [7–10], and even molecules [11,12]. These platforms are particularly versatile as they offer precise geometric shaping of arbitrary optical trapping potentials [13–16], thereby facilitating detailed control over the quantum state.

The manipulation of quantum systems makes use of energy and momentum transfer when light interacts with matter. Specific light fields such as Laguerre-Gaussian (LG) beams carry well-defined quanta of orbital angular momentum $l\hbar$ [17] (in addition to their intrinsic angular momentum determined by their polarization) and can induce a mechanical rotation in matter [18]. The transfer of orbital angular momentum from an LG beam to a macroscopic nanoparticle demonstrated the ability of light fields to exert torque [19]. Furthermore, the transfer of orbital angular momentum to a macroscopic quantum state forming a Bose-Einstein condensate showed the quantization of the angular momentum transfer [20]. However, the angular momentum control of a single neutral atom has remained elusive.

In this article we present an all-optical approach for injecting orbital angular momentum to a single atom by rotating an anisotropy of an optical tweezer. The precise control of the shape of the light field and its rotational speed, together with the small anharmonicity of the potential, enables us to selectively address motional states that differ in angular momentum and energy. In Fig. 1 we illustrate this process and show the in-plane tweezer potential, which approximately forms a two-dimensional (2D) harmonic potential with trap frequency ω . This work introduces a tool for quantum state engineering

and lays the groundwork for studies on interacting many-body systems in rapidly rotating optical traps [21].

II. ROTATING OPTICAL POTENTIALS

Our approach to create rotating optical traps is based on the interference of two Laguerre-Gaussian beams with waist W and electric field $\text{LG}_{0l}(r, \varphi) \propto (r/W)^{|l|} e^{il\varphi} e^{-r^2/W^2}$, where r and φ represent the polar coordinates. The main trap of the atoms is formed by a Gaussian LG_{00} beam, which is then interfered with a second LG_{0l} beam to induce rotation. The LG_{0l} mode carries $l\hbar$ quanta of orbital angular momentum, which is incorporated in the phase winding $e^{il\varphi}$ that breaks the rotational symmetry of the combined in-plane intensity pattern. Furthermore, by modulating the relative phase between both beams via the angular frequency detuning Ω we can engineer the time-dependent intensity distribution (see also Appendix A)

$$I(r, \varphi) = |\sqrt{P}\text{LG}_{00} - \sqrt{P_l}e^{-i\Omega t}\text{LG}_{0l}|^2 \sim [1 - \beta_l^* r^l \cos(l\varphi - \Omega t)]e^{-2r^2/W^2}. \quad (1)$$

Here P and P_l denote the power of the main tweezer and the perturbation beam, respectively, and β_l^* denotes the resulting strength of the interference term.

All light fields are formed via a spatial light modulator (SLM) in the Fourier plane of the atoms. In order to reduce optical phase aberrations stemming from the optical elements in the beam path such as the objective and the vacuum window, we measure the optical aberrations directly with the atoms via a phase-shifting interferometry algorithm [22,23].

A sketch of the SLM setup to generate rotating optical potentials is illustrated in Fig. 2(a). Two Gaussian laser beams (beam 1 in red and beam 2 in blue) are superimposed on the SLM under a nonzero relative angle. The phase pattern on the SLM forms two outgoing beams per incident beam [24], denoted by A and B. On beams A we choose a constant phase profile, leading to a Gaussian beam LG_{00} in the Fourier plane, while on beams B we imprint the $2\pi l$ phase winding,

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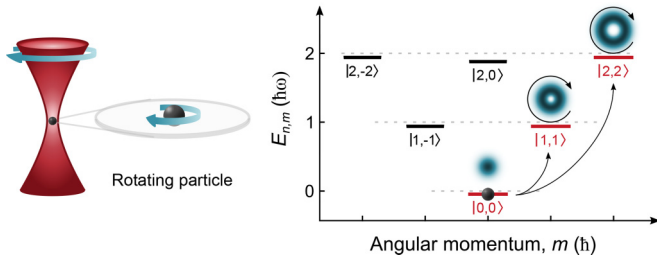


FIG. 1. Engineering angular momentum eigenstates. A single atom, prepared in the ground state of the optical tweezer, is set into rotation by the rotating external light field. The Gaussian trapping potential forms approximately a 2D harmonic oscillator with trap frequency ω . We label the states $|n, m\rangle$ by shell number n and angular momentum number m ; for the states with maximal angular momentum in each shell $n = m$ we show the state's density profiles, where the arrows indicate the phase winding. The rotating light field selectively couples the ground state to nonzero angular momentum states (black dashed arrows).

which approximately forms an l th-order LG mode LG_{0l} in the Fourier plane.¹ The relative angle between the outgoing beams is adjusted with the SLM such that two of the four beams are overlapped (beams 1A and 2B in Fig. 2). The other unwanted diffraction orders are spatially filtered with an iris in a Fourier plane behind the SLM, which is imaged on the plane of the atoms. Beam 1A constitutes the main optical tweezer, while beam 2B is the perturbation. In this configuration the SLM allows us to independently modify the local phase of the two overlapping outgoing beams. As both beams originate from different beams incident on the SLM, properties like beam power and global phase are individually addressable as well.

The speed of rotation is set by the relative angular frequency Ω of the tweezer and the perturbation beam, controlled via an acousto-optical modulator for each beam. This allows us to drive arbitrary frequency ramps, including a smooth increase of the rotation frequency or jumps. The optical trap geometrically rotates at rate Ω/l , which is l times slower than the frequency detuning between the beams. This reflects the l -fold symmetry of the LG_{0l} mode arising from its phase winding $2\pi l$. In Fig. 2(b) we show as an example the case of an LG_{02} mode which results in the elliptical shape of the trapping potential rotating with a rotation frequency $\Omega/2$.

III. COHERENT CONTROL OF ANGULAR MOMENTUM STATES

The experiment starts by loading a gas of ${}^6\text{Li}$ atoms from a magneto-optical trap into a red-detuned crossed optical dipole trap. After a sequence of radio-frequency pulses, we end up with a balanced two-component mixture of ${}^6\text{Li}$ in the hyperfine states $|F = 1/2, m_F = 1/2\rangle$ and $|F = 3/2, m_F = -3/2\rangle$;

¹The phase winding imprinted via the SLM enforces the outgoing beam to have a intensity depletion at its center. However, the exact radial distribution will deviate from that of an LG_{0l} mode. In general, the beam will be a superposition of LG_{kl} modes with differing k but fixed l .

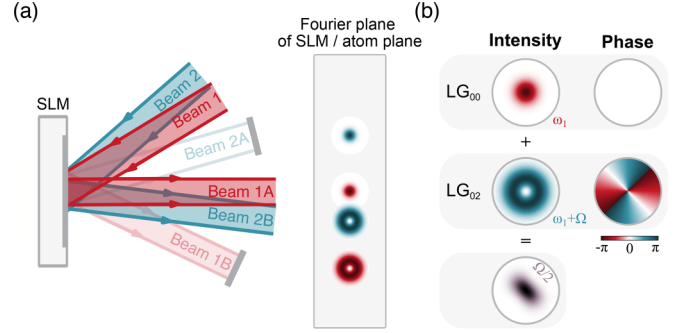


FIG. 2. Experimental setup to generate rotating optical potentials. (a) A spatial light modulator (SLM) is placed in the Fourier plane of the atom. By displaying an appropriate phase pattern on the SLM, we generate two outgoing beams A and B from a single incident beam with a different phase winding. Hence, two incident beams, beams 1 and 2, with a small relative angle with respect to each other, generate four outgoing beams. The SLM is used to overlap beam 1A forming the optical tweezer and beam 2B forming the perturbation, here displaced for clarity. (b) The tweezer is formed by a radially symmetric Gaussian beam. We imprint a phase winding on the perturbation beam to generate an LG mode of order l (here $l = 2$) in the atomic plane. The interference of the two beams creates an l -fold symmetric trap (for $l = 2$ an elliptically shaped trap). The relative frequency Ω between the interfering beams and the order l of the LG mode sets the rotation frequency Ω/l of the deformed potential. The optical frequency of the first beam is denoted by ω_1 .

in [21] they are referred to as spin up $|\uparrow\rangle$ and spin down $|\downarrow\rangle$, respectively. Next we load the atoms from the crossed optical dipole trap into a tightly focused cigar-shaped optical tweezer. We evaporate in the tweezer within 40 ms and reach a highly degenerate sample of roughly 200 atoms in total after evaporation. Subsequently, we use the spilling technique pioneered in [9] to prepare one spinup and one spin-down atom in the ground state of the optical tweezer with fidelities 95(3)%; the spilling procedure is performed at 300 G. We ramp the magnetic field to 568 G at which the spin states are noninteracting, which allows us to effectively consider a single atom in the ground state throughout the remaining paper (the other atom acts as an identical copy of the first one).

Our optical tweezer is formed by a Gaussian beam with waist $W \approx 1.1 \mu\text{m}$ and leads to an approximately harmonic potential with radial and axial trap frequencies of $\omega/2\pi \approx 28.1 \text{ kHz}$ and $\omega_{\text{ax}}/2\pi \approx 3.7 \text{ kHz}$, respectively. Since we prepare a single atom in the ground state and the rotation only couples to the radial motion of the atom, we neglect the axial degree of freedom. The in-plane potential in the harmonic expansion reads

$$V_{\text{pot}} = -V_0 e^{-2r^2/W^2} \sim \frac{m_{\text{Li}}\omega^2}{2} r^2 + O(r^4), \quad (2)$$

where V_0 denotes the potential depth of the tweezer, m_{Li} is the mass of ${}^6\text{Li}$, and the constant energy offset is neglected on the right-hand side of the equation. Corrections to the harmonic potential can be treated perturbatively, and we find that level shifts for the states interesting to the present work are on the order of several kilohertz (see Appendix B). We emphasize that the anharmonicity breaks the equidistance of the level

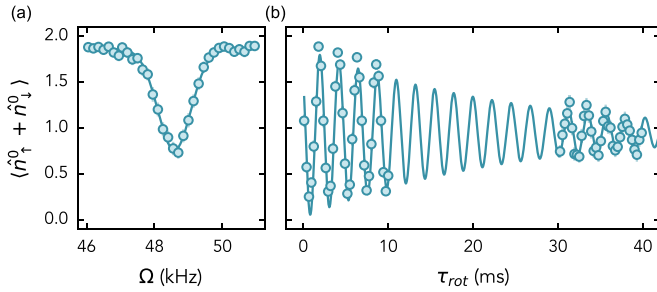


FIG. 3. Resonance spectrum and Rabi oscillations. (a) Resonance spectrum of the excitation from the ground state $|0, 0\rangle$ to the state $|2, 2\rangle$. The resonance is shifted down to $\Omega_{\text{res}} \approx 1.73\omega$ compared to 2ω due to the anharmonicity of the optical potential. (b) Rabi oscillations between the ground state $|0, 0\rangle$ and state $|2, 2\rangle$ with Rabi rates $\Omega_{\text{Rabi}}/2\pi \approx 0.44$ kHz and a coherence time $\tau_{\text{coh}} = 23(1)$ ms.

spacing in the harmonic trap, which enables closed transitions between two distinct states.

To reach states with nonzero angular momentum we use our all-optical approach described in the preceding section. Low-lying states in the trap (i.e., states that do not probe the Gaussian envelope of the perturbation beam) experience the rotating perturbation (see also Appendix A)

$$V_p = \beta_l r^l (e^{il\varphi} e^{-i\Omega t} + \text{H.c.}) \quad (3)$$

for an LG_{0l} mode and perturbation strength $\beta_l = V_0 \beta_l^*/2 \ll 1$. The perturbation couples the ground state $|0, 0\rangle$ to an angular momentum state $|n, m = l\rangle$; the coupling is resonant when $\hbar\Omega$ is equal to the energy difference between the states $E_{nm} - E_{00}$. To selectively address individual motional states, we make use of the anharmonicity to render the ground state $|0, 0\rangle$ and the state $|n, m\rangle$ a two-level system, in case the Rabi rate remains lower than the anharmonicity.

To demonstrate our exquisite control of preparing motional quantum states, we drive Rabi oscillations between $|0, 0\rangle$ and $|2, 2\rangle$. To determine the resonance frequency, we spectroscopically measure the single-particle occupation number in the ground state $\langle \hat{n}_{\uparrow}^0 + \hat{n}_{\downarrow}^0 \rangle$ after applying a rotating perturbation for $\tau = 350 \mu\text{s}$ at different rotation frequencies, shown in Fig. 3(a); here $\hat{n}_{\uparrow(\downarrow)}^0$ is the number operator for the spin-up (spin-down) particle in the ground state. We measure a resonance frequency $\Omega/2\pi \approx 48.59$ kHz, which corresponds to 1.73ω in units of the radial trap frequency ω . The resonance frequency is downshifted from 2ω due to the anharmonicity of the optical potential. Indeed, the observed frequency agrees well with the expected resonance based on first-order perturbation theory, which gives 1.75ω (cf. Appendix B). On resonance, we drive coherent oscillations between the ground state $|0, 0\rangle$ and the state $|2, 2\rangle$ [see Fig. 3(b)], with a Rabi rate $\Omega_{\text{Rabi}}/2\pi \approx 0.44$ kHz and a coherence time $\tau_{\text{coh}} = 23(1)$ ms significantly longer than the duration of a π pulse.

The precise control of angular momentum eigenstates requires us to overcome the following experimental challenges. First, the relative positions of the optical tweezer and the perturbation are required to be aligned on the order of the radial extent of the wave function, which in our case is typically around 200 nm. To this end, we use an LG_{00} mode as a resonant perturbation whose position is scanned across

the two-dimensional atom plane. By measuring the atom loss, we determine the relative position in the atom plane to approximately 100 nm. Second, the anisotropy $\delta\omega$ of the optical tweezer breaks the rotational symmetry of the system and sets an upper timescale $1/\delta\omega$ for the preparation of the angular momentum eigenstates (see the next section for details).

After preparing an angular momentum eigenstate, we release the atom from the tweezer and perform a time-of-flight expansion for $t_{\text{TOF}} = 2.5$ ms to measure the momentum of the atom using our single-atom fluorescence imaging technique [25]. In order to keep the atom within the depth of focus of our objective during the expansion, we rapidly turn on a 2D lattice with an axial confinement approximately matching the axial trap frequency of the optical tweezer. We note that this time-of-flight expansion is self-similar, reflecting the fact that the harmonic-oscillator wave functions have the same shape in their position and momentum space representation. We reconstruct the 2D momentum density distribution of the first three angular momentum eigenstates $|0, 0\rangle$, $|1, 1\rangle$, and $|2, 2\rangle$ by taking 10 047, 3398, and 7998 snapshots of the wave function, shown in Figs. 4(a)–4(c), respectively. While all densities exhibit a rotationally symmetric distribution, the nonzero angular momentum states show the expected density depletion at zero momenta and a maximum at $\sqrt{m}p_{\text{HO}}$, with the momentum scale in harmonic-oscillator units being $p_{\text{HO}} = \sqrt{\hbar m_{\text{Li}} \omega}$.

To quantitatively compare the measured distribution to the eigenstates of the 2D harmonic oscillator, we determine the radial densities n_p by azimuthally averaging over the obtained 2D densities, shown in the bottom row of Fig. 4 for the respective angular momentum state $|m, m\rangle$. We find good agreement between the fit-free theoretical curve and our experimental data. The largest deviations occur at small momenta, which we attribute to an imperfect π -pulse excitation caused by fluctuations of the trap frequency (below 1%), which leaves the atom in the ground state and therefore contributes to the density at zero momenta.

IV. TIME EVOLUTION OF ANGULAR MOMENTUM STATES

To confirm that the central depletion of the density distribution stems from a phase winding given by the imprint of angular momentum, we investigate the time evolution of the state $|2, 2\rangle$ in an anisotropic potential. In a radially symmetric trap an angular momentum state is an eigenstate of the Hamiltonian. However, in an anisotropic potential the angular momentum states become a superposition of the true eigenstates of the system and thus evolve in time. We make use of a small residual anisotropy present in the optical potential which we attribute to a slight ellipticity of the tweezer. The new effective energy eigenstates of this system are then formed by $|\pm\rangle = 1/\sqrt{2}(|2, 2\rangle \pm |2, -2\rangle)$ with an energy difference defined as the anisotropy $\delta\omega$ (for details see Appendix C). The states $|\pm\rangle$ form a two-level system, which can be depicted on the Bloch sphere, shown in Fig. 5(a). Therefore, for the $|2, 2\rangle$ state we expect a characteristic time evolution oscillating between the $|2, 2\rangle$ and $|2, -2\rangle$ states.

We perform Ramsey spectroscopy on the state $|2, 2\rangle$ and observe coherent oscillations with a frequency given by the

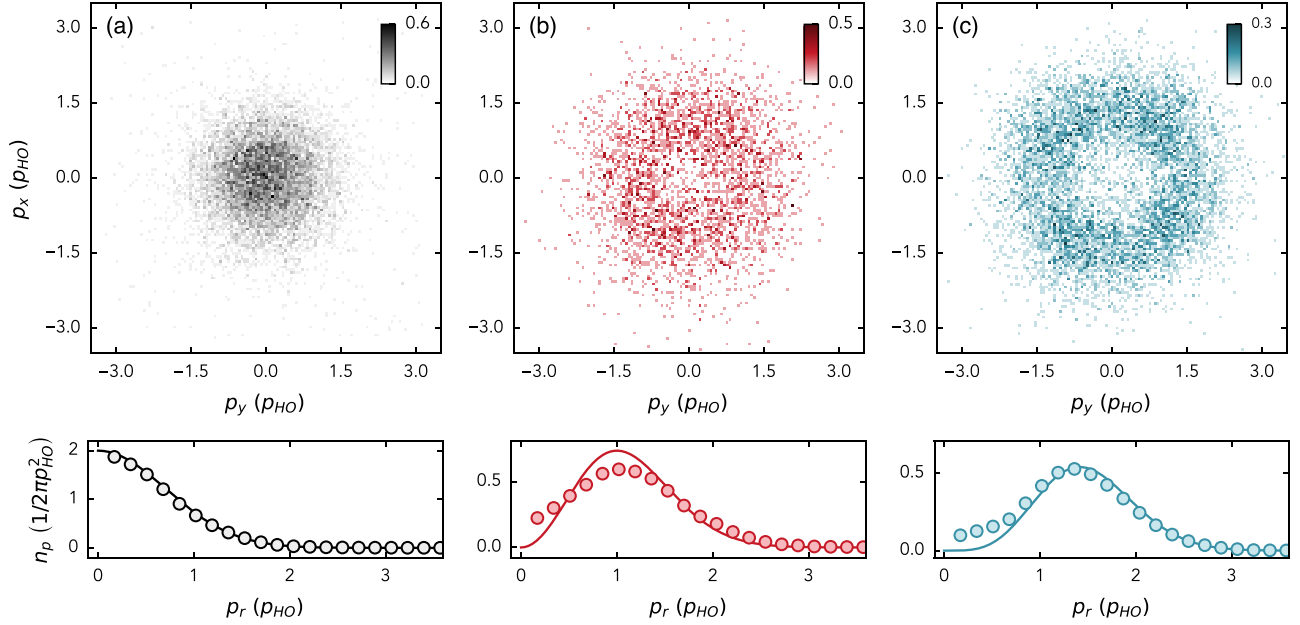


FIG. 4. Single-atom angular momentum eigenstates. Shown on top is the normalized two-dimensional momentum-space density distribution and on the bottom the azimuthally averaged radial density of (a) the ground state $|0, 0\rangle$ with zero angular momentum and states with nonzero angular momentum (b) $|1, 1\rangle$ and (c) $|2, 2\rangle$. The solid lines in the bottom row are theoretical calculations without free parameters.

anisotropy $\delta\omega$. In Fig. 5(b) we outline the experimental protocol. We use a π pulse to inject $2\hbar$ quanta of angular momentum (gray solid arrow). Subsequently, we let the system evolve for a delay time τ_R (red arrows), after which we use a second π pulse to deexcite the evolved state to the ground state (gray dashed arrow). We measure the

single-particle occupation number in the ground state $\langle \hat{n}_\uparrow^0 + \hat{n}_\downarrow^0 \rangle$ in Fig. 5(c), which oscillates with the energy difference given by the anisotropy $\delta\omega/2\pi = 27.3(4)$ Hz. This yields a relative anisotropy $\delta\omega/\omega = 9.6 \times 10^{-4}$. The state is evolving on a timescale much longer than the duration of the π pulse, which sets the timescale on which we prepare and detect the

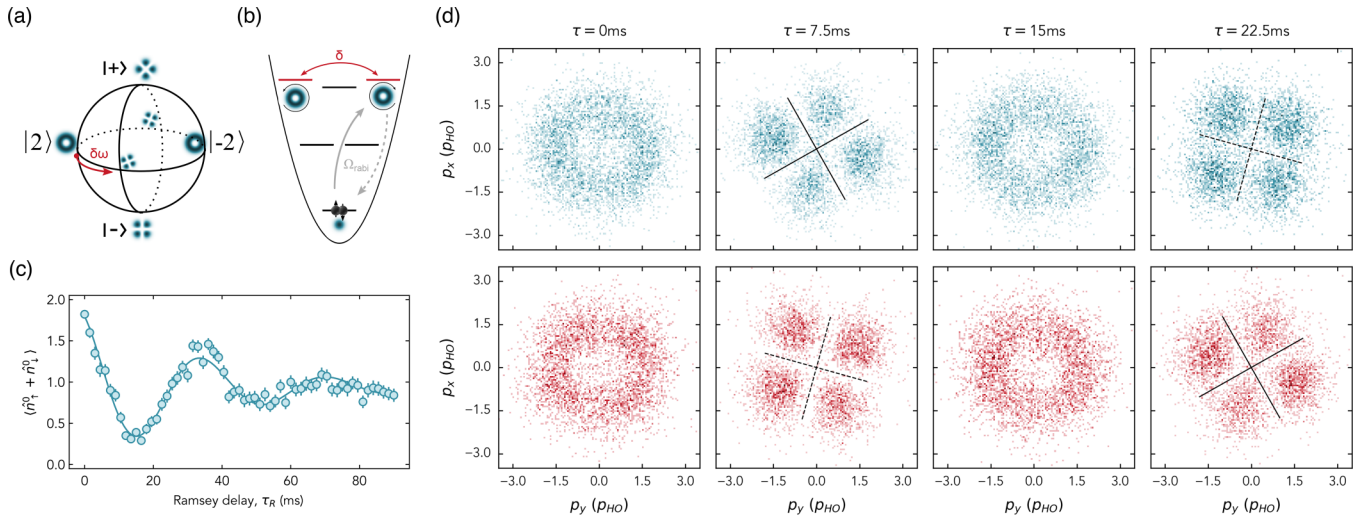


FIG. 5. Ramsey spectroscopy. (a) In the presence of anisotropy, the superposition states $|\pm\rangle = 1/\sqrt{2}(|2, 2\rangle \pm |2, -2\rangle)$ form the new eigenstates of the system with an energy difference given by the anisotropy $\delta\omega$. The initialized state $|2, 2\rangle$ is an equal superposition of the eigenstates $|+\rangle$ and $|-\rangle$ and hence evolves over time τ_R on the equator of the Bloch sphere. (b) The anisotropy couples states which differ in angular momentum. We harness this effect to perform Ramsey spectroscopy by preparing the state $|2, 2\rangle$ via a π pulse, followed by a Ramsey delay time τ_R and a second π pulse to deexcite the atoms to the ground state. Depending on the contribution of the $|2, -2\rangle$ state, the overlap with the ground state oscillates. (c) Ramsey spectrum of the state $|2, 2\rangle$. We measure an anisotropy of $\delta\omega/2\pi = 27.3(4)$ Hz at a trap frequency $\omega/2\pi \approx 28.1$ kHz, yielding a relative anisotropy $\delta\omega/\omega = 9.6 \times 10^{-4}$. The coherence time is $\tau_{\text{coh}}^{(\text{nonint})} = 35(3)$ ms. The amplitude oscillates between two and zero atoms as we have two identical (noninteracting) copies of the same state in the tweezer. (d) Normalized density distribution of clockwise (top row) and counterclockwise (bottom row) evolving states at different evolution times.

state $|2, 2\rangle$. The coherence time of the Ramsey oscillations is $\tau_{\text{coh}}^{(\text{nonint})} = 35(3)$ ms. We argue that this timescale is limited by noise of experimental parameters, predominantly the trap depth, leading to loss of coherence via coupling to other energy levels in the trap. We expect the coherence time to be strongly dependent on the noise spectrum and levels close to the targeted state. Indeed, we observe a significant increase in coherence time when energy eigenstates close to the prepared state are shifted away, as demonstrated in the related Letter [21].

In Fig. 5(d) we show the 2D density distribution after preparing the $|2, 2\rangle$ state and letting it evolve in the slightly anisotropic optical potential for different quarter periods of the Ramsey delay time. The density evolves from the $|2, 2\rangle$ state at $\tau = 0$ to an equal superposition of the $|2, \pm 2\rangle$ states at $\tau = T/4$; it continues to the $|2, -2\rangle$ state at $\tau = 2T/4$ and further evolves again to a superposition of the $|2, \pm 2\rangle$ states at $\tau = 3T/4$, however, now tilted by 45° with respect to the state at $\tau = T/4$ (black dashed cross). By reversing the phase winding on the SLM, we prepare the $|2, -2\rangle$ state, which starts the precession on the Bloch sphere from another starting point. Thereby, it confirms the imprint of the expected phase winding of $\pm 2 \times 2\pi$, which corresponds to an angular momentum of $2\hbar$.

We further observe a slight deviation from the expected densities at $\tau = T/4, 3T/4$ (nonvanishing center density connecting one pair of lobes diagonally), which we attribute to a weak coherent admixture of the $|2, 0\rangle$ state that mediates the effective time evolution between the $|2, \pm 2\rangle$ states (cf. Appendix C).

V. CONCLUSION

We have demonstrated motional control of angular momentum eigenstates of a single atom in an optical tweezer. By interfering the optical tweezer with an LG beam of order $l = m$, we coherently coupled the ground state to a nonzero angular momentum eigenstate $|m, m\rangle$. We confirmed the preparation of the angular momentum eigenstates by measuring the 2D densities and by observing the evolution of the state in a slightly anisotropic trap. The latter allowed us to reveal the phase imprint on the wave function through density measurements at different times. Beyond the control of the single-particle angular momentum eigenstates, this technique enables the studies of ultracold atoms in optical potentials subjected to synthetic magnetic fields [26], including the recent realization of a two-particle Laughlin state [21].

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APPENDIX A: INTERFERENCE OF LAGUERRE-GAUSSIAN BEAMS

The electric field of a Laguerre-Gaussian beam of order l , and waist W at its focus is given by

$$\text{LG}_{0l}(r, \varphi, z = 0) = \sqrt{\frac{2}{\pi l! W^2}} \left(\frac{\sqrt{2}r}{W} \right)^l e^{il\varphi} e^{-r^2/W^2}. \quad (\text{A1})$$

To create a rotating optical potential, we interfere the light beam of the main tweezer, a Gaussian LG_{00} mode with power P , with a Laguerre-Gaussian beam LG_{0l} mode with power P_l , resulting in the intensity distribution

$$\begin{aligned} I(r, \varphi) &= |\sqrt{P}\text{LG}_{00} - \sqrt{P_l}\text{LG}_{0l}|^2 \\ &= \frac{2P}{\pi W^2} e^{-2r^2/W^2} \left| 1 - \sqrt{\frac{P_l}{P}} \left(\frac{\sqrt{2}r}{W} \right)^l e^{il\varphi} \right|^2. \end{aligned} \quad (\text{A2})$$

High-intensity seeking atoms experience the potential

$$\begin{aligned} V(r, \phi) &= -V_0 e^{-2r^2/W^2} + \beta_l r^l (e^{il\phi} + e^{-il\phi}) e^{-2r^2/W^2} \\ &\quad - \frac{1}{V_0} \beta_l^2 r^{2l} e^{-2r^2/W^2}, \end{aligned} \quad (\text{A3})$$

via the optical dipole force, where $V_0 = \gamma P/W^2$, $\gamma \approx 800h$ kHz $\mu\text{m}^2/\text{mW}$, and $\beta_l = \gamma \sqrt{2^l P P_l}/W^{l+2}$. Here the first term gives rise to a harmonic confinement at first order, with trapping frequency $\omega = 2W^{-2} \sqrt{\gamma P/m_{\text{Li}}}$ and length scale $l_0 = \sqrt{\hbar}/m_{\text{Li}}\omega$. As usual, we are interested in the regime in which the harmonic approximation applies, i.e., $l_0 \ll W$, and further in which the harmonic confinement is dominant, i.e., $\beta_l l_0^l/\hbar\omega \ll 1$. Additionally, we assume $\sqrt{2^l P_l/P}(l_0/W)^l \ll 1$ such that the β^2 term may be neglected. Finally, by coherently altering the phase of the Laguerre-Gaussian beam according to $e^{-i\Omega t}$, we obtain Eq. (3),

$$V_p = \beta_l r^l (e^{il\varphi - i\Omega t} + \text{c.c.}). \quad (\text{A4})$$

Note that Rabi rates between the harmonic-oscillator states introduced by the rotating perturbation are on the order of $\beta_l l_0^l/\hbar$.

APPENDIX B: ANHARMONIC LEVEL SHIFTS

The Gaussian potential in harmonic-oscillator units can be rewritten according to

$$V = \frac{1}{2}r^2 - \frac{1}{2g}(e^{-gr^2} - 1) - \frac{1}{2}r^2 \equiv \frac{1}{2}r^2 + V_{\text{anh}}, \quad (\text{B1})$$

where $g = 2l_0^2/W^2 \approx 0.099$ in our case. We are primarily interested in states $|m, m\rangle$ of the harmonic oscillator, which in real space are described by the wave function $\varphi_{m,m}(r, \phi) = \sqrt{\frac{1}{\pi m!}} r^m e^{im\phi} e^{-r^2/2}$. In first-order perturbation theory such states experience an energy shift of

$$\begin{aligned} \Delta V_{\text{anh}} &= \frac{1}{2g} \left(1 - \frac{1}{(1+g)^{m+1}} \right) - \frac{1}{2}(m+1) \\ &\approx -\frac{1}{4}(m+2)(m+1)g, \end{aligned} \quad (\text{B2})$$

where $\langle m, m | e^{-gr^2} | m, m \rangle = (1 + g)^{-(m+1)}$ and $\langle m, m | r^2 | m, m \rangle = m + 1$ were used. We note that the expansion in g of Eq. (B2) is equivalent to the expansion of the Gaussian potential in orders of r^2 . We find that the first order in g is sufficient for the states considered in this work.

APPENDIX C: ANISOTROPIC COUPLING

Here we provide details on the effective coupling of the state $|2, 2\rangle$ due to the presence of the remaining ellipticity of the optical tweezer, illustrated in Fig. 6. We can incorporate this ellipticity into the Gaussian trap model by inserting a factor $e^{-2\epsilon(x^2-y^2)/W^2}$ into the potential (2) which breaks the azimuthal symmetry. At first order in ϵ it introduces a perturbation term proportional to $r^2 e^{i2\varphi} + \text{H.c.}$ that couples states with $\Delta m = \pm 2$ with a generic state-dependent coupling δ_2 linear in ϵ . Similarly, a term proportional to $r^4 e^{i4\varphi} + \text{H.c.}$ appears at second order in ϵ (neglecting isotropic terms) and couples states with $\Delta m = \pm 4$ with coupling δ_4 . Therefore, at first order, states of the $\pm 2\hbar$ angular momentum manifold are coupled to states with $0\hbar$ quanta of angular momentum, and only at second order, there is direct coupling between states in the $\pm 2\hbar$ angular momentum manifold. Due to the anharmonicity of the optical trap, the accessible $|2, 0\rangle$ state is detuned from the $|2, 2\rangle$ and $|2, -2\rangle$ states by $\Delta' \gg \delta_2$, which is on the order of kilohertz. Hence, we expect an effective coupling $\delta_4 - \delta_2^2/\Delta' \sim \epsilon^2$ only between the degenerate clockwise

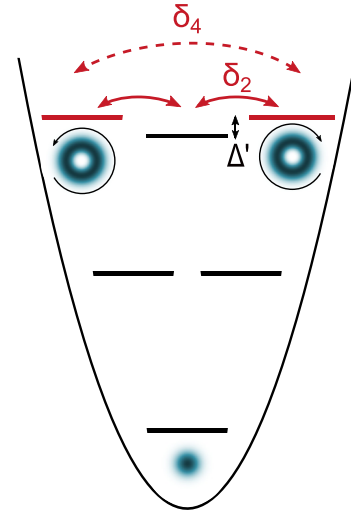


FIG. 6. Anisotropic coupling. The anisotropy breaks the azimuthal symmetry of the optical tweezer, leading to a coupling of states with $\Delta m = \pm 2$ to first order and $\Delta m = \pm 4$ to second order in ϵ (see the text for details).

and counterclockwise rotating states. The new effective energy eigenstates are given by $|\pm\rangle = 1/\sqrt{2}(|2, 2\rangle \pm |2, -2\rangle)$. The energy difference between the eigenstates is defined as the anisotropy $\delta\omega \approx 2\delta_4 - 2\delta_2^2/\Delta'$. The states $|\pm\rangle$ then effectively form a two-level system.

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